





CS221

- It is instructive to compare Gibbs sampling with its cousin, Iterated Conditional Modes (ICM). Both iteratively go through the variables and tries to update each one of them holding the others fixed. • Recall that the goals are different: ICM tries to find the maximum weight assignment while Gibbs sampling is trying to compute marginal
- probabilities
- Accordingly, ICM will choose the value for a variable X<sub>i</sub> with the highest weight, whereas Gibbs sampling will use the weights to form a distribution to sample from.
  ICM converges to local optimum, an assignment that can't be improved on. Note that Gibbs sampling is stochastic so in some sense never
- ICM converges to local optimum, an assignment that can be improved on. Note that clobs sampling is stochastic so in some sense never converges. In the owner, the estimates of the marginal probabilities do in fact converges under some technical assumptions. The simplest sufficient condition if all weights are positive, but it also suffices that the probability of Gibbs sampling going between any two assignments is positive. A major cavaet is that the time it takes to converge can be exponential in the number of variables.
   Advanced: Gibbs sampling is an instance of a Markov Chain Monte Carlo (MCMC) algorithm which generates a sequence of particles X<sup>(1)</sup>, X<sup>(2)</sup>, X<sup>(2)</sup>, X<sup>(3)</sup>, ..., A Markov chain is irreducible if there is positive probability of getting from any assignment to any other assignment (now the probability source the random choices of the sampler). When the Gibbs sampler is irreducible, then in the limit as t → ∞, the distribution of X<sup>(t)</sup> converges to the true distribution P(X). MCMC is a very rich topic which we will not talk about very much here.

• In summary, we are trying to compute the marginal probabilities of a Markov network

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- Gibbs sampling allows us to do this by exploring all the assignments randomly, but very carefully controlled probabilities, so that the visitation frequencies of various values converge to the right answer.
   Gibbs sampling is part of a beautiful and rich set of tools for using randomness to do inference on Markov networks, which I encourage you to check out.