





- Let's add a constraint that says we can't visit three odd cities in a row. If we only keep track of the current city, and we try to move to a next city, we cannot enforce this constraint because we don't know what the previous city was. So let's add the previous city into the state.
 This will work, but we can actually make the state smaller. We only need to keep track of whether the previous city was an odd numbered to be the state.
- Note that in doing so, we have 2n states rather than n^2 states, which is a substantial savings. So the lesson is to pay attention to what information you actually need in the state.

- Our first thought might be to remember how many odd cities we have visited so far (and the current city).
- But if we're more clever, we can notice that once the number of odd cities is 3, we don't need to keep track of whether that number goes up to 4 or 5, etc. So the state we actually need to keep is (min(number of odd cities visited, 3), current city). Thus, our state space is O(n) rather than O(n²).
 We can visualize what augmenting the state does to the state graph. Effectively, we are copying each node 4 times, and the edges are
- We can result and the source of the state of the state graph. Encentry, we are copying each note 4 times, and the oges are redirected to move between these copies.
 Note that some states such as (2,1) aren't reachable (if you're in city 1, it's impossible to have visited 2 odd cities already); the algorithm will not touch those states and that's perfectly okay.

Å in chat

Question

Objective: travel from city $1 \mbox{ to city } n$, visiting more odd than even cities. What is the minimal state?

- An initial guess might be to keep track of the number of even cities and the number of odd cities visited.
 But we can do better. We have to just keep track of the number of odd cities minus the number of even cities and the current city. We can write this more formally as (n₁ n₂, current city), where n₁ is the number of odd cities visited so far and n₂ is the number of even cities visited so far.

